

Geometry and Algebra with Transformations
Algebra One Review

Equation Solving

1. $\frac{3}{7}x - 12 = 30$

$$\frac{7}{3} \left(\frac{3}{7}x = 42 \right) \frac{7}{3}$$

$$\boxed{x = 98}$$

2. $\frac{4}{11}x + 23 = x - 19$

$$-\frac{4}{11}x + 19 = -\frac{4}{11}x + 19$$

$$42 = \frac{7}{11}x$$

$$\left(\frac{11}{7}\right)42 = x$$

$$\boxed{66 = x}$$

3. $4 - 8(x - 4) = 2 + 6(3 - x)$

$$4 - 8x + 32 = 2 + 18 - 6x$$

$$-8x + 36 = 20 - 6x$$

$$-2x = -16$$

$$\boxed{x = 8}$$

4. $2\{3 - 4(3x - 6)\} = 12$

$$2\{3 - 12x + 24\} = 12$$

$$2\{27 - 12x\} = 12$$

$$54 - 24x = 12$$

$$-24x = -42$$

$$\boxed{x = -1.75}$$

5. $(x - 3)^2 = 81$

$$x - 3 = \pm 9$$

$$x - 3 = 9 \quad x - 3 = -9$$

$$x = 12 \quad x = -6$$

6. $13 = \frac{5}{13}(4 - 2x)^2$

$$\frac{169}{5} = (4 - 2x)^2$$

$$\pm 5.81 \approx 4 - 2x$$

$$5.81 \approx 4 - 2x \quad -5.81 \approx 4 - 2x$$

$$1.81 \approx -2x \quad -9.81 \approx -2x$$

$$\boxed{-0.91 \approx x}$$

$$\boxed{4.91 \approx x}$$

Systems of Equations

7. $5x + 7y = 11$
 $8y - 4x = 100$

$$20x + 28y = 44$$

$$-20x + 40y = 500$$

$$\hline 68y = 544$$

$$y = 8$$

$$5x + 7(8) = 11$$

$$5x + 56 = 11$$

$$5x = -45$$

$$x = -9$$

$$\boxed{(-9, 8)}$$

8. $y = 6 - 5x$
 $6y - 12 = 3(2x + 4y)$

$$6y - 12 = 6x + 12y$$

$$-6y - 12 = 6x$$

$$\hline 6$$

$$-y - 2 = x$$

$$y = 6 - 5(-y - 2)$$

$$y = 6 + 5y + 10$$

$$-4y = 16$$

$$y = -4$$

$$-(-4) - 2 = x$$

$$2 = x$$

$$\boxed{(2, -4)}$$

9. $2(3x + 5y) = 4x - 36$
 $4 - 5(3x + y) = 11y - 21$

$$6x + 10y = 4x - 36$$

$$2x + 10y = -36$$

$$\hline 2$$

$$x + 5y = -18$$

$$4 - 15x - 5y = 11y - 21$$

$$-15x - 16y = -25$$

$$\hline 15x + 75y = -270$$

$$\boxed{(7, -5)}$$

$$59y = -295$$

$$y = -5$$

$$x + 5(-5) = -18$$

$$x = 7$$

Exponents

10. $(2x + 4)(4x - 9)$
 $8x^2 - 18x + 16x - 36$
 $8x^2 - 2x - 36$

11. $(2x + 4)^2$
 $(2x + 4)(2x + 4)$
 $4x^2 + 8x + 8x + 16$
 $4x^2 + 16x + 16$

12. $(4x^6)^2$
 $16x^{12}$

13. $(3x^4)^3$
 $27x^{12}$

14. $\frac{20x^6}{5x^3}$
 $4x^3$

15. $\frac{20x^6}{30x^{10}}$
 $\frac{2}{3x^4}$

16. $x^5 + x^5$
 $2x^5$

17. $x^5 - x^5$
 0

18. $(x^5)^5$
 x^{25}

19. $(x^5)(x^5)$
 x^{10}

20. $3x^2(2x - 5)^2$
 $3x^2(2x - 5)(2x - 5)$
 $3x^2(4x^2 - 10x - 10x + 25)$
 $12x^4 - 60x^3 + 75x^2$

21. $(4x^5)(-6x^{10})$
 $-24x^{15}$

22. $(3x^4)(2x^6)^3$
 $(3x^4)(8x^{18})$
 $24x^{22}$

Writing Equations of Functions

23. Write the equation of a line that contains the point $(-9, 4)$ with a slope of $\frac{1}{6}$

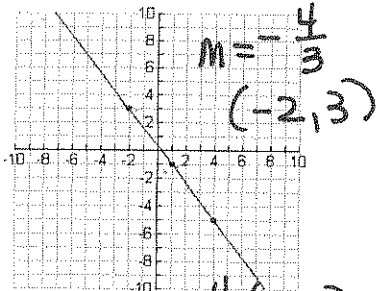
$$y - 4 = \frac{1}{6}(x + 9)$$

24. Write the equation of a line that contains the points $(-5, 9)$ and $(5, -10)$

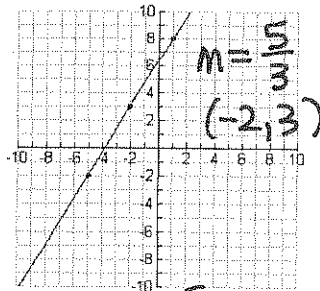
$$m = \frac{\Delta y}{\Delta x} = \frac{9 - (-10)}{-5 - 5} = \frac{19}{-10}$$

$$y - 9 = \frac{19}{-10}(x + 5)$$

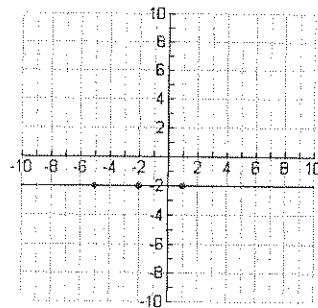
25. Write the equation of these lines



$$y - 3 = -\frac{4}{3}(x + 2)$$



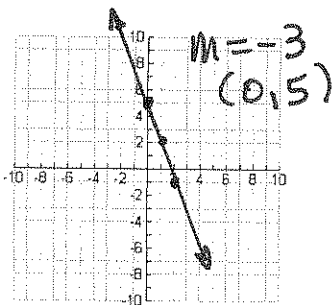
$$y - 3 = \frac{5}{3}(x + 2)$$



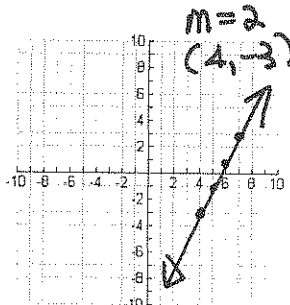
$$y = -2$$

26. Graph these functions

A. $y = -3x + 5$



B. $y + 3 = 2(x - 4)$



C. $y = \frac{-2}{5}(x + 3)$

